

八年级数学(下)周末作业(十二) 五一假期作业 20250501 1-7 BDDDBBB 8.4;3;2 9. $x \geq 1$ 且 $x \neq 2$ 10.-3 11.2
12.2 分之 9 13. $m < 3$ 且 $m \neq 2$ 分之 3 14.1 或 -2 15. $2y - y$ 分之 $3 = 2$ 16.2023 17.b-a 分之 a+b 18.x=5 19.-1 20.2.5(以
CE 为边作等边 $\triangle CEH$,连 FH,则 $\triangle CEG \cong \triangle EFH$,当 $FH \perp AB$,FH 小=2.5 21(1)a+b (2)x+3 分之 1 (3)x-1 分之 1 (4)x+1 分之 x (5)x+3
分之 1 (6)a+b 分之 2b 22(1)2 根号 2 (2)4 (3)9-2 根号 5 23(1)无解 (2)x=-3 分之 4 (3)x=-5 24(1)化简得 a-1 分之 a,当 a=2,
原式=2 (2)5 分之 1 祝同学们假期愉快!

(1) ① $\because xy = 1$,

$$\therefore \frac{1}{1+x^2} + \frac{1}{1+y^2} = \frac{xy}{xy+x^2} + \frac{xy}{xy+y^2} = \frac{xy}{xy+x^2} + \frac{xy}{xy+y^2} = \frac{x(y+x)}{xy} + \frac{y(x+y)}{xy} = \frac{x+y}{xy} = \frac{x+y}{1} = 1$$

 故答案为: 1
 ②证明: $\because xy = 1$,
 $\therefore x^{2021}y^{2021} = 1$,

$$\therefore \frac{1}{1+x^{2021}} + \frac{1}{1+y^{2021}} = \frac{x^{2021}y^{2021}}{x^{2021}y^{2021}+x^{2021}} + \frac{1}{1+y^{2021}} = \frac{x^{2021}y^{2021}}{x^{2021}(y^{2021}+1)} + \frac{1}{1+y^{2021}} = \frac{y^{2021}}{1+y^{2021}} + \frac{1}{1+y^{2021}} = \frac{y^{2021}+1}{1+y^{2021}} = 1$$

 (2) $\because \frac{x}{y+z} + \frac{y}{z+x} + \frac{z}{x+y} = 1$, 且 $x+y+z \neq 0$,

$$\therefore \frac{x}{y+z} = 1 - \frac{y}{z+x} - \frac{z}{x+y}$$

$$\therefore \frac{x^2}{y+z} = x - \frac{xy}{z+x} - \frac{xz}{x+y}$$

 同理可得: $\frac{y^2}{z+x} = y - \frac{xy}{y+z} - \frac{yz}{x+y}$,

$$\frac{z^2}{x+y} = z - \frac{xz}{y+z} - \frac{yz}{z+x}$$

$$\therefore \frac{x^2}{y+z} + \frac{y^2}{z+x} + \frac{z^2}{x+y} = (x - \frac{xy}{z+x} - \frac{xz}{x+y}) + (y - \frac{xy}{y+z} - \frac{yz}{x+y}) + (z - \frac{xz}{y+z} - \frac{yz}{z+x})$$

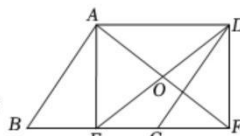
$$= x + y + z - (\frac{xy}{z+x} + \frac{xz}{x+y} + \frac{xy}{y+z} + \frac{yz}{x+y} + \frac{xz}{y+z} + \frac{yz}{z+x})$$

$$= x + y + z - (\frac{xz+yz}{x+y} + \frac{xy+xz}{y+z} + \frac{xy+yz}{z+x})$$

$$= x + y + z - [\frac{(x+y)z}{x+y} + \frac{(y+z)x}{y+z} + \frac{(x+z)y}{z+x}]$$

$$= x + y + z - (x + y + z) = 0$$

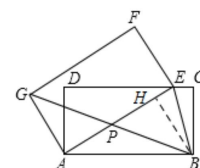
(1)证明: $\because$ 四边形 ABCD 是平行四边形,
 $\therefore AD \parallel BC, AD = BC$
 $\therefore CF = BE$,
 $\therefore CF + CE = BE + CE$
 $\therefore EF = BC$,
 $\therefore AD \parallel EF$,
 $\therefore$ 四边形 AEFD 是平行四边形,
 $\therefore AE \parallel EF$,
 $\therefore \angle AEF = 90^\circ$,
 $\therefore$ 四边形 AEFD 是矩形.
 (2)由 (1) 知: 四边形 AEFD 是矩形,
 $\therefore AF = DE = 2OE = 2 \times 2 = 4$,
 $\therefore AB = 3, BF = 5$,
 $\therefore AB^2 + AF^2 = BF^2$,
 $\therefore \triangle ABF$ 是直角三角形,
 $\therefore \triangle ABF$ 的面积 = $\frac{1}{2} BF \cdot AE = \frac{1}{2} AB \cdot AF$,
 $\therefore 5 \times AE = 3 \times 4$,
 $\therefore AE = 2.4$.



(1) $\because$ 矩形 ABCD 中, $\angle CBA = 90^\circ$,
 $\therefore \angle CBE + \angle ABE = 90^\circ$,
 即 $2\angle CBE + 2\angle ABE = 180^\circ$, ①
 由旋转可得, $AB = AE$,
 $\therefore \angle ABE = \angle AEB$,
 $\therefore \angle BAE + 2\angle ABE = 180^\circ$, ②
 由①②可得, $\angle BAE = 2\angle CBE$,
 $\therefore \angle CBE = \frac{1}{2} \angle BAE$;

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(2)如图, 过 B 作 $BH \perp AE$ 于 H, 则 $\angle C = \angle BHE = 90^\circ$,
 由 (1) 可得, $\angle ABE = \angle AEB$,
 $\therefore AB \parallel CE$,
 $\therefore \angle ABE = \angle CEB$,
 $\therefore \angle BEC = \angle BEH$,
 即 BE 平分 $\angle CEH$,
 $\therefore BH = BC$,
 由旋转可得,
 $AG = AD = BC$,
 $\angle GAP = \angle BAD = 90^\circ$,
 $\therefore AG = HB$,
 $\angle GAP = \angle BHP$,
 又: $\angle APG = \angle HPB$,
 $\therefore \triangle APG \cong \triangle HPB$,
 $\therefore GP = BP = \frac{1}{2} BG$,
 即 $BG = 2PB$;

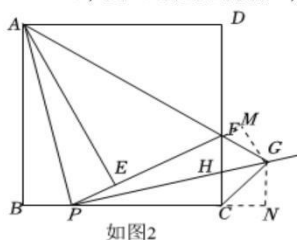


(1) $\because$ 四边形 ABCD 是正方形,
 $\therefore AB = AD, \angle BAD = \angle B = \angle D = 90^\circ$,
 $\therefore$ 点 B 关于直线 AP 的对称点为 E,
 $\therefore AB = AE, \angle B = \angle AEP = 90^\circ, \angle BAP = \angle PAE$,
 $\therefore \angle AEF = \angle D = 90^\circ, AE = AD$,
 在 $Rt\triangle EAF$ 与 $Rt\triangle DAF$ 中,

$$\begin{cases} AE = AD \\ AF = AF \end{cases}$$

 $\therefore Rt\triangle EAF \cong Rt\triangle DAF (HL)$,
 $\therefore \angle DAF = \angle EAF$,
 $\therefore \angle PAE + \angle EAF = \frac{1}{2} \angle BAD = 45^\circ$,

故答案为: 45° ;
 (2)过点 G 作 $GM \perp EF$, 交 EF 的延长线于点 M,
 $HN \perp BC$, 交 BC 的延长线于点 N,



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如图2
 $\therefore$ 点 B 关于直线 AP 的对称点为 E,
 $\therefore AB = AE, \angle APB = \angle APE$,
 $\therefore PG$ 平分 $\angle FPC$,
 $\therefore \angle CPG = \angle FPG$,
 $\therefore \angle APG = \frac{1}{2} \angle BEC = 90^\circ$,
 $\therefore \angle PAG = 45^\circ$,
 $\therefore \angle PAG = \angle AGP$,
 $\therefore AP = PG$,
 $\therefore \angle APB + \angle GPN = 90^\circ, \angle BAP + \angle APB = 90^\circ$,
 $\therefore \angle BAP = \angle GPN$,
 $\therefore \angle ABP = \angle PGN = 90^\circ$,
 $\therefore \triangle ABP \cong \triangle PGN (AAS)$,
 $\therefore BP = GN$,
 $\therefore PG$ 平分 $\angle CPF, GM \perp EF, GN \perp BC$,
 $\therefore MG = GN$,
 $\therefore S_{\triangle APF} = \frac{1}{2} PF \cdot AE, S_{\triangle PFG} = \frac{1}{2} PF \cdot GM$,
 $\therefore \frac{S_{\triangle APF}}{S_{\triangle PFG}} = \frac{AE}{GM} = \frac{4}{1} = 4$,
 $\therefore \frac{AB}{BP} = 4$,
 $\therefore AB = 3$,
 $\therefore BP = \frac{3}{4}$.